Practical and Dynamic Attribute-Based Keyword Search Supporting Numeric Comparisons Over Encrypted Cloud Data

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Abstract—The attribute-based keyword search (ABKS), which simultaneously achieves searching and fine-grained access control over encrypted data, is frequently applied in cloud computing environments characterized by data storage and sharing. Recently, inspired by attribute-based encryption (ABE) and searchable encryption (SE) primitives, several ABKS schemes have been presented. However, almost all existing ABKS schemes actually only provide an attribute-based keyword equality match function and do not have a structural index to support practical search efficiency and dynamic data updates in real-world applications. To the best of our knowledge, this study is the first to realize an attribute-based keyword search construction supporting numerical comparison expressions with the practical search efficient and dynamic data update capacity (ABKS-NICEST), based on our proposed attribute-based keyword secure search scheme supporting numerical comparison expressions (ABKS-NICE) and an exclusive OR-chain-based inverted index structure. To the best of our knowledge, ABKS-NICEST is the first attributed-based keyword search scheme with practical search efficiency and dynamic data update capacity. In addition, numerical values are an important and common attribute, so providing comparison expressions among numerical values can greatly enhance the expressivity of access policy. Therefore, we use the prefix membership verification technique to design a method to support any numeric comparison expression in a flexible and uniform manner. Through theoretical and experimental evaluations, we determine that ABKS-NICEST is the most efficient ABKS scheme.

Index Terms—Attribute-based keyword search, cloud computing, data security and access control, dynamic data update, practical search efficiency

1 INTRODUCTION

1.1 Motivation

The enormous advantages of cloud computing have driven numerous enterprises and individuals to outsource applications and data to cloud platforms. The end-users are able to access applications and data through mobile devices anytime and anywhere. However, the security of cloud computing is always a controversial issue as storing data to cloud platforms also means that data owners discard the control power of their data. Without a sturdy protection measure, the malicious attackers including even the cloud server self can easily obtain the outsourced data [1]. Encryption before uploading data to the cloud server is most effective way to guarantee the confidentiality of data [2]. A challenging problem is how to efficiently perform operations over ciphertext exactly like being in the plaintext domain without decrypting them. It is critical for cloud applications, as the cloud computing is characterized by not only massive data storage, but efficient data processing.

A number of studies has been conducted to achieve operations directly over ciphertext, among which searchable encryption is a recently vibrant research field, aiming at guaranteeing both confidentiality and searchability over encrypted data. Song et al. [3] presented the first practical searchable encryption construction. Subsequent researches [4], [5] devoted to persistently refining the search complexity and security, even explored the more practical dynamic schemes [6], [7], [8] supporting secure data addition and deletion. As all these constructions were built in the symmetric key system, they are referred to as searchable symmetrical encryption (SSE).

In practical, access control is a required mechanism to prevent data from being illegally accessed by unauthorized entities, especially in the data-sharing cloud environment. This practical requirement has broken new ground in designing searchable encryption with data access control, called attribute-based keyword search (ABKS) [9]. Such
solutions [10], [11], [12], [13], [14], [15] are able to achieve private search and fine-grained access control simultaneously in the ciphertext environment, inspired by attribute-based encryption [16] and searchable encryption. However, so far almost all existing ABKS schemes just provide an attribute-based keyword equality test functionality. How to employ them in real-world data set with practical search efficiency is still unknown. Meaningfully, these researches provide a theoretical conclusion for the technical feasibility of the attribute-based searchable encryption.

Inspired by searchable encryption, Work [13] and [14] equipped their ABKS with inverted index on the real-world data set, as shown in Fig. 1, where each encrypted keyword involves an access policy specifying its search permission and $\text{id}_n$ denotes the identifier of a file data containing keyword $w$. Though thus a construction can obtain search results from real world data set, it still suffers from an impractical search efficiency.

When a search query is issued, the search algorithm linearly scans encrypted keywords in such a way that for each keyword it has to first performs a search authorization as long as the search query has access to the keyword, followed by the private textual match between the search query and current keyword according to the intermediate result produced by the search authorization. Unfortunately, the search authorization based on ABE systems involves time-consuming public-key operations such as pairings and exponentiations. Though being able to obtain data files containing a certain search query, the simple index construction may lead to many redundant search authorizations that incur a long search process. For example, there is a super data user that has the search permissions of all index keywords. Some point in time, when she issues a search query with respect to the last keyword $w_n$ in the index, $(n - 1)$ search authorizations have to be conducted one by one, which introduces a large number of time-consuming pairing and exponentiation operations. More generally, if we refer to the index keywords that a search query can access as its the authorization keyword set (AKS), the average of needed pairing and exponentiation operations increases linearly with the size of AKS, which will become a performance bottleneck of this construction. Also, this is a simple static construction unsuitable for the real-world cloud application, without a mechanism to update data dynamically. Motivated by these limitations, in this paper, for the first time, we realize a practically efficient and dynamic ABKS construction based on our proposed exclusive-OR chain. The construction can ensure that the heavy search authorization is only performed one time at most regardless of the size of AKS, as well as the dynamic data and keyword search permission update. To the best of our knowledge, ABKS-NICEST is the first attributed-based keyword search scheme with practical search efficient and dynamic data update.

In addition, as few original ABE systems have focused on numerical value comparisons in access policies, almost all ABKS schemes do not consider the widely existing numeric comparison expression. Number is a kind of very important and common attribute in the practical application. For example, policy ("DOCTOR" OR "PROFESSOR") AND "COMPUTER SCIENCE" AND "30≤age≤50" AND "level>5") indicates that only person who is a doctor or a professor and works in the department of computer science and whose age is between 30 and 50 with the supervisory level greater than 5 can access the corresponding ciphertext. A naive approach to deal with the numeric comparison expressions "30≤age≤50" and "level>5" is to enumerate all values within these two ranges and express them using OR gates, i.e., "age=30 OR 31... OR 50" and "level=6 OR 7... OR max," where $\text{max}$ may be a reasonably preset value to denote the maximum of the attribute level. Obviously, such an expression is impractical when the value space is large. In this paper, we propose to use the prefix membership verification technique to convert the numeric comparison expression into the equivalent OR gate policy and realize the match between a numerical attribute and the converted policy. Our approach can greatly reduce the number of OR gates and can be used by all ABE and ABKS schemes as an building-block to express numeric attribute comparisons.

1.2 Contributions
We make the following four contributions.
1. Based on the efficient and provably secure ABE scheme by Waters [17], we construct an Attribute-Based Keyword secure Search scheme supporting Numerical Comparison Expressions, named ABKS-NICE. Functionally, similar to existing ABKS schemes, ABKS-NICE is just an attribute-based keyword equality test scheme. However, except for supporting numerical comparison expressions, ABKS-NICE uses more general LSSS representation and has better efficiency due to the lesser pairing operations.
2. We design an inverted index construction based on encrypted XOR chain. Combining it and ABKS-NICE, for the first time, we propose the Attribute-Based Keyword Search construction supporting Numerical Comparison Expressions with the practical Search efficient and dynamic data update capacity, ABKS-NICEST.
3. We use the prefix membership verification technique to realize an approach in ABE or ABKS systems that can support any numerical attribute comparison operation in a flexible and uniform manner.
4. We provide formal security proofs and extensive experiments for ABKS-NICE and ABKS-NICEST. The evaluation results show that ABKS-NICEST is a truly practical ABKS scheme over the real-world data set.

We believe that the technical contribution of ABKS-NICEST is to provide a feasible research line for the practical and dynamic attribute-based keyword search.
2 RELATED WORK

2.1 Searchable Encryption

In [18], Chase and Kamara proposed the concept of the structured encryption. As its a particular case, searchable encryption has plentiful research results, recently. Song et al. [3] designed the first practical SSE and later Chang and Mitzenmacher [4] proposed a construction achieving forward privacy. The search time cost of both of them is linear in the size of the data files. It was not until 2006 when the SSE construction that achieves sub-linear search complexity was designed by Curtomla et al. [5]. They first proposed to use encrypted inverted index structure to speed up search process. Since then, the encrypted inverted index becomes a core data structure for designing efficient and practical SSE. In order to be applicable in real-word cloud storage systems, SSE was further extended to a dynamic environment, allowing for the dynamic and secure data addition and deletion [6], [7], [8].

Due to recently developed file injection attacks [19], the dynamic SSE constructions with forward privacy have been intensively researched [20], [21], [22], [23], [24]. The forward privacy guarantees that updating a document does not leak more information than what a predefined leakage function leaks and thus makes the file injection attack ineffective. Backward privacy is another stronger security notion. It requires that a search query does not reveal information from data that were deleted. Several SSE schemes achieving backward privacy are also proposed in [25], [26].

2.2 Attribute-Based Encryption and Attribute-Based Keyword Search

Sahai and Waters proposed the first attribute-based encryption scheme in [16]. Goyal et al. [27] and Bethencourt et al. [28] introduced more expressive attribute-based encryption by using tree based access policy. The former is a KP-ABE, which means the access policy is embedded into the key and the ciphertext is associated with a set of attributes. On the contrary, the later is that the access policy is in the ciphertext and the key is described by attributes, referred to as a CP-ABE. No matter what construction you choose, a successful decryption has to require that the attributes satisfy the access policy. Many variants of ABE were proposed to acquire more excellent properties, such as multiple authorities [29] and hidden access structure [30].

Recently, in order to make the encrypted cloud data searchable with the flexible data access control, combining ABE and SE, a number of ABKS schemes are proposed in [10], [11], [12], [13], [14], [15]. However, these ABKS schemes just provide an attribute-based keyword equality test functionality and are short of effective index mechanism for a practical search efficiency in the real application. Though work [14] constructed a new index by simply associating each encrypted keyword with data files containing the keyword to speed up the search process, without a full-fledged index structure, it still suffers from impractical search efficient in practice due to redundant and expensive search authorizations.

To enhance the expressivity of ABE scheme, authors [28] first considered to deal with numeric comparison expression in the access policy and transformed an integer comparisons into AND and OR gate policies over “bag of bits” divided by a numeric comparison expression. However, this transformation is relatively complex, resulting in the inefficiency. In order to degrade the complexity, Xue et al. [31] used only OR gates to convert access policies of numeric comparison expressions by using 0-encoding and 1-encoding technique. Though this scheme considers two inequality operations “>” and “<”, it is defective to support other widely used relationships such as “≠”, “≥”, “≤”, etc.

3 PRELIMINARIES

In this section, we introduce several techniques used in our schemes, including Bilinear Pairing Map [16], Access Structure [28], Linear Secret Sharing Scheme (LSSS) [17], Prefix Membership Verification [32], Pseudo Random Function [5]. We present the detailed descriptions about these techniques in Appendix A.

4 PROBLEM FORMULATIONS

Our attribute-based keyword search problem is based on a service-oriented cloud computing outsourcing environment, as shown in Fig. 2, where the cloud server provides powerful data storage and computation services. Roughly speaking, the cloud server provides a service to store outsourced encrypted data and secure index; if the cloud server receives an outsourced computation request, it will provide the corresponding computation services such as data searching or data updating based on ciphertexts. Our service-oriented computation model fully embodies the idea of “Service Computing,” including “Storage-as-a-Service,” “Software-as-a-Service,” and “Security-as-a-Service”. We will describe a more detailed system model in Section 4.1.

4.1 System Model

Our system model is illustrated in Fig. 3, in which three entities are involved. In order to make the outsourced data secure and searchable, before uploading the data, the data owner (DO) encrypts data using a symmetric encryption and construct searchable secure index using a CP-ABE scheme with access polices. Via secure communication channels, DO sends secret key with attributes to a data user.
to be 8 bits, converting a numeric comparison expression only needs 14 prefixes \((1011\ OR\ 11**))\). Thus, expression “10 < C < 16” is converted to a range \([11,15]\), whose upper bound is a linear function of \(h\). Currently, we solve it by solving the prefix family of 12. Due to the high cardinality of attributes, the naive approach based on numerical value enumeration technique tells us that if \(n\) is in \(R\), there exists a common prefix in \(S(R)\) and \(PF(n)\). Thus, we convert the problem of whether a numerical attribute satisfies a numeric comparison policy to the verification of whether exists a common prefix in \(S(R)\) and \(PF(n)\).

Table 1 shows numeric comparison expressions and corresponding transformed ranges, where \(max\) and \(min\) are reasonable values to denote the maximum and the minimum of an attribute. For example, for attribute \(age\), we can set \(max\) and \(min\) to be 0 and 100. Naturally, for expressions \(v_1 < attr < v_2\) and \(v_1 \leq attr < v_2\), the transformed ranges are \([v_1 + 1, v_2 - 1]\) and \([v_1, v_2]\), respectively.

**Example.** To help understand how our idea works, we give a concrete example. Consider an access policy “A AND (B OR 10 < C < 16)” of non-numeric attributes. First, “10 < C < 16” is converted to a range \([11,15]\), where \(n\) represents the natural number. Then, we compute the minimum set of prefixes \(S([11,15]) = \{1011,11**\}\). Next, the transformed access policy can be represented as “A AND (B OR (1011 OR 11**))”. Thus, expression “10 < C < 16” is converted to an equivalent policy of an OR gate with two prefix strings. Finally, we convert it to the corresponding LSSS matrix by a standard algorithm [29]. The access tree and the LSSS matrix are shown in Fig. 4.

Suppose that a decryptor has an attribute set \(\{A, C=12\}\), which can be converted to the attribute set \(\{A, 1100, 110^*, 11**, 1***, ****\}\) by solving the prefix family of 12. Due to having attributes “A” and “11**,” the decryptor can decrypt a ciphertext encrypted under the policy “A AND (B OR (1011 OR 11**)”.

**Remark.** Obviously, converting a comparison expression to the minimum set of prefixes actually increases the number of attributes, resulting in the extension of rows of the LSSS matrix. Theoretically, it will increase both storage and computation cost of the LSSS matrix. Fortunately, given a range \([v_1, v_2]\), its minimum set of prefixes \(S([v_1, v_2])\) contains at most \(2h - 2\) prefixes [33], where \(h\) denotes the bit length of \(v_1\) and \(v_2\), whose upper bound is a linear function of \(h\). This is a very nice feature. Further, for all possible intervals \([v_1, v_2]\), if we assume all the intervals appear with the same probability, the average number of prefixes in \(S([v_1, v_2])\) is equal to \(\frac{(h-2)2^{2h+1}+h(12^2+1)}{2^{2h+1}+h2^h+1}\), which is approximately equal to \(h - 2\) [34]. For example, if we set \(h\) to be 8 bits, converting a numeric comparison expression only needs 14 prefixes (attributes) and 13 OR gates in the worst case. As a comparison, the naive approach based on numerical value enumeration produces 128 attributes and 127 OR gates in the worst case (0 \(\leq\ attr \leq 127\).
6 ABKS-NICE

6.1 Construction

ABKS-NICE consists of SetUp, Enc, KeyGen, TokenGen, Search five algorithms. We describe the algorithm implementation in Fig. 5.

The work flow of ABKS-NICE incorporated into a service-oriented cloud computing environment is illustrated in Fig. 6. Though ABKS-NICE supports flexible numeric comparison expression policy, it only achieves the attribute-based textual matching between two encrypted keyword. Like existing ABKS schemes, it is still unknown to apply ABKS-NICE on real data set to facilitate practically efficient data searching and dynamic data updating. As the fundamental building block, ABKS-NICE will be integrated into ABKS-NICEST to achieve a truly practical, dynamic, and attribute-based searchable encryption.

6.2 Correctness

Theorem 1. Given a ciphertext \( T_w \) of keyword \( w \) and LSSS matrix \((A, \rho)\) and a search token \( T_Q \) of query keyword \( Q \) and attribute set \( U \), if \( U \) satisfies \((A, \rho)\) and \( w = Q \), the search algorithm Search will return true.

Proof. First, if \( U \) satisfies \((A, \rho)\), we can find a subset \( I \subset \{1, 2, \ldots, |S|\} \) and a set of constants \( \{\omega_i \in \mathbb{Z}_p^* \}_{i \in I} \) such that \( \sum_{i \in I} \omega_i A_i = (1, 0, \ldots, 0) \), where \( I \) is defined as \( I = \{i : \rho(i) \in U\} \). Further, the algorithm computes

\[
e((I_w)I_2, (T_Q)T_1) = (g^s, g^{\rho H_I(Q)} g^{\rho \omega H_I(Q)} \prod_{i \in I} (e((I_w)C_i, (T_Q)T_2)e((I_w)D_i, (T_Q)T_{\rho(i)}))^{\omega_i} = e(g, g^{\rho H_I(Q)}) e(g^s, g^{\rho \omega H_I(Q)}) = e(g, g)^{\omega H_I(Q)} e(g, g)^{\rho \omega H_I(Q)}
\]

and

\[
\prod_{i \in I} \left( e((I_w)C_i, (T_Q)T_2)e((I_w)D_i, (T_Q)T_{\rho(i)}))^{\omega_i} = e(g^s, g^{\rho H_I(Q)}), e(g^s, g^{\rho \omega H_I(Q)}), e(g, H_1(\rho(i))^{\omega H_I(Q)}), e(g, H_1(\rho(i))^{\omega \omega H_I(Q)}), e(g, H_1(\rho(i))^{\omega H_I(Q)}), e(g, H_1(\rho(i))^{\omega \omega H_I(Q)})
\]

Therefore, we have

\[
e((I_w)I_2, (T_Q)T_1) = e\left(\prod_{i \in I} e((I_w)C_i, (T_Q)T_2)e((I_w)D_i, (T_Q)T_{\rho(i)}))^{\omega_i} e(g, g)^{\omega H_I(Q)} e(g^s, g^{\rho \omega H_I(Q)})
\]

The proof is completed. \( \Box \)

6.3 Performance

Functionally, similar to the existing ABKS schemes [10], [11], [12], [13], [14], [15], (which were constructed over the access tree structure based ABE scheme of Bethencourt et. al. [28] and have asymptotically same computation complexity), ABKS-NICE is only an attribute-based keyword equality match scheme without providing the data index construction for real-world data set. However, ABKS-NICE has better match efficiency as the required pairing operations are less than that of the above mentioned schemes. Moreover, ABKS-NICE uses more general LSSS representation with better expressivity as well as supports numerical comparison expressions. We will conduct the theoretical and experimental evaluations of the algorithms in ABKS-NICE with the new scheme ABKS-NIEST together in Sections 7 and 8.

6.4 Security

Inspired by the security proof technique present in ABE scheme by Waters [17], we adopt the reduction idea to prove the security of ABKS-NICE. Loosely speaking, proving ABKS-NICE’s security will be reduced to try to solve the decisional q-parallel Bilinear Diffie-Hellman Exponent problem [17]. However, the decisional q-parallel BDHE problem is acknowledged intractable in the polynomial time. Here, in brief, we review the decisional q-parallel BDHE problem/assumption as follows.

Let \( G, G_T \) be cyclic groups of prime order \( p \) and \( g \) be a generator of group \( G \). The Decisional \( q \)-Parallel BDHE problem is defined that an adversary \( A \) has non-negligible advantage \( \epsilon \) to solve decisional \( q \)-parallel BDHE problem if

\[
\Pr[A(\overline{x}, M) = e(g, g)^{g^{\overline{x}+1}}] = \Pr[A(\overline{x}, M = R) = 0] \geq \epsilon,
\]

where \( \overline{x} = (g, g, g^s, g^{s+y}, g^{s+y} g^{s+y}, \ldots, g^{s+y} g^{s+y}, \ldots, g^{s+y} g^{s+y}, \ldots, g^{s+y} g^{s+y}) \)

and \( x, s, y, \ldots, y \in \mathbb{Z}_p^* \) are chosen at random, \( R \) is randomly chosen from \( G_T \). The decisional \( q \)-parallel BDHE assumption indicates that there is no adversary that can solve this problem within the polynomial time.
Also, we adopt the standard security model in the ABKS scheme, namely Adaptively Chosen-Keywrdt Attack model, which is formalized by the following game between a Chal-

\[ \begin{align*}
\mathcal{P} &\leftarrow \text{SetUp}(\mathbb{1}^l): \text{When we input a sufficiently large security factor } l, \text{ the algorithm chooses two multiplication cyclic groups } G, G_T \text{ of the order } p. \text{ Choose a generator } g \in G \text{ and two random exponents } \alpha, x \in \mathbb{Z}_p^\times. \text{ Define a computationally efficient bilinear map } e : G \times G \rightarrow G_T \text{ and two hash functions } H_1 : \{0, 1\}^* \rightarrow G, H_2 : \{0, 1\}^* \rightarrow \mathbb{Z}_p. \\
\text{Finally, the algorithm outputs the public parameter } \mathcal{P} = (G, G_T, H_1, H_2, g, g^*, e(g, g)^{\alpha}) \text{ and master key } \mathcal{MK} = (x, \alpha).
\end{align*} \]

\[ \begin{align*}
\mathcal{I}_w &\leftarrow \text{Enc}(\mathcal{P}, r, w): \text{The DO runs the algorithm to encrypt a keyword. When we input a keyword } w, \text{ an access policy } \tau \text{ with a set of attributes } S, \text{ and the system parameter } \mathcal{P}, \text{ the algorithm encrypts } w \text{ as follows:} \\
&\quad \text{First, if } \tau \text{ contains } \ell > 0 \text{ comparison expressions(s) with numerical attributes } q_1, \ldots, q_\ell, \text{ it is converted into } \ell \text{ ranges } R_1, \ldots, R_\ell; \text{ the minimum set of prefixes } \{S(R_i)\}_{1 \leq i \leq \ell} \text{ and } S := \bigcup_{1 \leq i \leq \ell} ((S - q_i) \cup S(R_i)) \text{ is then computed; and } \\
&\quad \tau \text{ is transformed by replacing each comparison expression with OR gates among prefixes in } S(R_i). \\
&\quad \text{Second, the algorithm generates the LSSS matrix of } \tau \text{ as } (A, \rho), \text{ where } A \text{ is a } |S| \times n \text{ matrix; extend } s \text{ to } y = (s, y_2, \ldots, y_n) \text{ for random } y_2, \ldots, y_n, \text{ and for } i = 1 \text{ to } |S|, \text{ calculate } A_i = \forall A_i. \\
&\quad \text{Finally, it randomly chooses } r_1, \ldots, r_{|S|} \in \mathbb{Z}_p^\times \text{ and encrypts } w \text{ as} \\
&\quad \mathcal{I}_w = \left\{ \begin{array}{l}
I_1 = e(g, g)^{\alpha H_2(w)}, I_2 = g^a \\
(C_i = g^{r_i} H_1(\rho(i))^{-r_i}, D_i = g^{r_i})_{1 \leq i \leq |S|}
\end{array} \right. \\
\text{In this encryption, the access policy } \tau \text{ implicitly specifies who has the search permission to the keyword } w.
\end{align*} \]

\[ \begin{align*}
\mathcal{K} &\leftarrow \text{KeyGen}(\mathcal{U}, \mathcal{MK}): \text{The DO runs the algorithm to generate a private key for a specified attribute set } \mathcal{U}. \text{ When we input a set of attributes } \mathcal{U}, \mathcal{P}, \text{ the algorithm chooses a random } t \in \mathbb{Z}_p^\times \text{ and computes} \\
&\quad \mathcal{K} = \left\{ \begin{array}{l}
k_1 = g^a, k_2 = g^{r_1}, k_3 = g^t \\
\forall u \in \mathcal{U} : k_u = H_1(u)^t
\end{array} \right. \\
\text{Data users who have the attribute set } \mathcal{U} \text{ can use } \mathcal{K} \text{ to encrypt a query keyword on which they want to perform search. Note that if } \mathcal{U} \text{ contains a numerical value } v, \text{ the algorithm needs to calculate } P.F(v) \text{ and } \mathcal{U} \leftarrow (\mathcal{U} \cup v) \cap F(v). \end{align*} \]

\[ \begin{align*}
\mathcal{T}_Q &\leftarrow \text{TokenGen}(\mathcal{K}, \mathcal{Q}): \text{The DU runs the algorithm to encrypt a query keyword } \mathcal{Q}. \text{ When we input } \mathcal{K} \text{ and } \mathcal{Q}, \text{ the algorithm chooses a random element } \theta \in \mathbb{Z}_p^\times \text{ and encrypts } \mathcal{Q} \text{ as} \\
&\quad \mathcal{T}_Q = \left\{ \begin{array}{l}
T_1 = (k_1 k_2) H_2(\mathcal{Q}) = g^{\alpha H_2(\mathcal{Q})} g^{\theta H_2(\mathcal{Q})} \\
T_2 = (k_3)^{H_2(\mathcal{Q})} = g^{\theta H_2(\mathcal{Q})} \\
\forall u \in \mathcal{U} : T_u = (k_u)^{H_2(\mathcal{Q})} = H_1(u)^{H_2(\mathcal{Q})}
\end{array} \right. \\
\text{An authorized DU with the attribute set } \mathcal{U} \text{ runs the algorithm to output the search token } \mathcal{T}_Q = (T_1, T_2, \{T_u\}_{u \in \mathcal{U}}) \text{ of any query keyword } \mathcal{Q}.
\end{align*} \]

\[ \begin{align*}
\text{true or false } &\leftarrow \text{Search}(\mathcal{I}_w, \mathcal{T}_Q): \text{When we input a search token } \mathcal{T}_Q \text{ and an encrypted keyword } \mathcal{I}_w, \text{ if } \mathcal{U} \text{ hidden in } \mathcal{T}_Q \text{ satisfies the } |S| \times n \text{ LSSS matrix } (A, \rho) \text{ in } \mathcal{I}_w, \text{ the algorithm can find a subset } I \subseteq \{1, 2, \ldots, |S|\} \text{ and a set of constants } \{\omega_i \in \mathbb{Z}_p^\times\}_{i \in I} \text{ such that } \Sigma_{i \in I} \omega_i A_i = (1, 0, \ldots, 0), \text{ where } I \text{ is defined as } I = \{i : \rho(i) \in \mathcal{U}\}. \text{ The algorithm further computes} \\
&\quad A = e((\mathcal{I}_w), (\mathcal{T}_Q); T_1) \prod_{i \in I} e((\mathcal{I}_w), C_i, (\mathcal{T}_Q); T_2) e((\mathcal{I}_w), D_i, (\mathcal{T}_Q); T_{\rho(i)})^{\omega_i}
\end{align*} \]

Finally, it verifies
\[ A = I_w I_1 \]

When receiving token \( \mathcal{T}_Q \) from a DU, CS invokes the algorithm to perform an equality test between \( \mathcal{T}_Q \) and \( \mathcal{I}_w \) without learning the underlying plaintexts of \( w \) and \( \mathcal{Q} \).

If the equation above holds, this indicates a successful match (\( \mathcal{U} \) satisfies \( (A, \rho) \) and \( w = \mathcal{Q} \)), and the algorithm returns true.

However, if the algorithm returns false, at least one of the following two conditions holds:

- \( w \neq \mathcal{Q} \);
- There does not exist a subset \( I \subseteq \{1, 2, \ldots, |S|\} \) and a set of constants \( \{\omega_i \in \mathbb{Z}_p^\times\}_{i \in I} \) such that \( \Sigma_{i \in I} \omega_i A_i = (1, 0, \ldots, 0) \) (i.e., \( \mathcal{U} \) does not satisfy access policy \( (A, \rho) \)).

The second condition also declares that the DU has no search permission for the keyword \( w \).

Fig. 5. The construction of ABKS-NICE.
KeyGen has the search permission to wind is issued, the server first performs a search permission containing /C8 and f to obtain ABKS-NICE’s public is about to be added in the corre-
X/C20 and f be a pseudo-random and ð/C8 and S A: exclusive-OR chain 1/C20 BKS denotes f; /C8; w/c if Oð before and re-attaches T w w and 1 with entity is selected uniformly at random from a finite set ST X/C20 implies an access policy determining who have corresponding to a requested trapdoor. is the system security parameter. Notation TrapGen ind A G runs an algorithm /C8 X A Oð¼ and ind !f/C8 T to a
TrapGen !f/C2f with entity
1 responds the ciphertext with B c 1 b is only a value. and ¼ Q 1 H Phase 1. and are maintained by the client and the server, between a client and a
tokens corresponding list, the client first computes two secure update
server deletes
hash table at location w
ð and YIN ET AL.: PRACTICAL AND DYNAMIC ATTRIBUTE-BASED KEYWORD SEARCH SUPPORTING NUMERIC COMPARISONS OVER... 2861
Fig. 6. The workflow of ABKS-NICE.

- OKeyGen(P, S i): B runs an algorithm KeyGen to estab-
lish the private key K i (1 ≤ i ≤ n) and sends it to A.
- OTrapGen(K i, Q i): B runs an algorithm TrapGen to
establish the query trapdoor T Q i (1 ≤ i ≤ n) and
sends it to A.

Challenge. A chooses a challenging LSSS matrix A∗ and
two keywords w0 and w1, which are sent to B. The restric-
tion is that if S i (1 ≤ i ≤ n) satisfies A∗, then w0, w1 /∈ {Q i , · · · , Q n }, B randomly picks up a bit b ∈ {0, 1} and encrypts w b with A∗. OEnc responds the ciphertext T w b to A.

Phase 2. A repeats Phase 1. There is a restriction that if an
attribute set S i corresponding to a requested trapdoor T Q i , satisfies A∗, then w0, w1 /∈ Q. i.

Guess. A outputs a guess b of b.

The advantage that a PPT adversary A wins the game is
defined as Adv =Pr[b = b ] − 1/2.

Theorem 2. Given the one-way secure hash H 2, when modeling H 1
as a random oracle, the proposed ABKS-NICE is secure against
ACKA under the decisional q-parallel BDHE assumption.

Refer to Appendix B to find the complete proof.

7 ABKS-NICEST

7.1 Main Idea

Our basic goal is to achieve attribute-based and dynamic
searchable encryption with practical search complexity. In
this section, we design ABKS-NICEST by employing the
classic inverted index-based structural framework and
ABKS-NICE scheme. In ABKS-NICEST construction, we
propose the exclusive-OR chain to be able to dynamically
form the inverted list of a keyword w with O(1) keyword
authorization search. At a high level, when a new file (iden-
tifier) ind w containing w is about to be added in the corre-
sponding list, the client first computes two secure update
tokens T w and T w+1 based on a locally maintained counter c, which
counts the current number of files matching w before inserting
ind w+1, and then computes T w ⊕ T w+1 and the
encryption version ind w+1 of ind w+1. c is incremented and
(Tw, Tw+1, Tw ⊕ Tw+1, ind w+1) is sent to the server. After receiv-
ing the update information, the server needs to perform two
operations. One is to store (Tw ⊕ Tw+1) along with ind w+1 to a
hash table at location Tw+1. The second operation is that the
server deletes w’s search permission denoted by ϕ w from
entity at location T w and re-attaches ϕ w with entity T w+1, where ϕ w implies an access policy determining who have permission to search with w.

When a search query with respect to the search token T w+1 is issued, the server first performs a search permission verification between T w+1 and ϕ w (search authorization). If T w+1 has the search permission to w, then it is arrowed to obtain ind w+1 and (Tw + Tw+1); by computing (Tw + Tw+1), Tw is obtained subsequently leading to ind w and (Tw+1 + Tw), and iteratively the server obtains all file identifiers until meets a sentinel T w0 which are sent to the client as search results; otherwise, the search returns nothing.

Fig. 7 shows the main idea of proposed ABKS-NICEST scheme. To place the ABKS scheme in the practice, the most essential goal is to let the computational complexity of the heavy attribute-based search authorization achieve O (1), regardless of the size of data files and keywords. We achieve this goal by designing the XOR chain construction and letting search permission of a keyword only associate with the latest entity to be added in the chain. Thus, in a search process, the search authorization can be performed at most one time. Meanwhile, thanks to XOR
chain, the dynamic update of files and correct search can be achieved.

7.2 Construction

In essence, our proposed ABKS-NICEST is a combination of
the ABKS scheme ABKS-NICE and a dynamic SSE scheme based on XOR chain index construction. We use the standard
SSE protocol framework to describe ABKS-NICEST construction implementation. Formally, ABKS-NICEST consists
of three polynomial-time protocols ABKS-
NICEST= (Setup, Update, Search) between a client and a
server.

Let F : {0, 1} k × {0, 1} λ → {0, 1} λ be a pseudo-random
function, and H 3 : {0, 1} k × {0, 1} λ → {0, 1} λ and H 1 : {0, 1} k × {0, 1} λ → {0, 1} λ are two keyed hash functions, and ψ : {0, 1} λ → {0, 1} λ are one-way hash function, where k is the system security parameter. Notation a ⊕ X denotes that a is selected uniformly at random from a finite set X and notation a → X (or X → a) denotes that a is the output
of algorithm X, or X is assigned to a if X is only a value. Finally, we use notation Γ to denote the proposed ABKS-
NICE scheme.

Setup(k, 1⊥). The client takes a security parameter k as
input, the algorithm generates a system master key K and
invokes Γ.Setup and Γ.KeyGen to obtain ABKS-NICE’s public parameter, master key, and private key. Two empty hash
tables CT ST are maintained by the client and the server,
respectively. Algorithm 1 provides a pseudo-code description of setup implementation.

Algorithm 1. Setup(k; ⊥)

Input: security parameter k
Output: system master key K, ABKS-NICE’s public parameter P, master key MK, private key K, and two hash tables CT, ST
Client: $s$
1: $K \leftarrow \{0, 1\}^k$
2: $\Gamma = \{(3, i, r, H_1, H_2, g, g', e(g, g')), MK = \{x, a\} \leftarrow \Gamma$.Setup
3: $K = (k_1 \rightarrow g, k_2 \rightarrow g', k_3 \rightarrow g', \{k_5 \rightarrow H_3(u,h')_{w(i)}\}) \leftarrow \Gamma$.KeyGen
4: CT $\leftarrow$ empty hash table
5: ST $\leftarrow$ empty hash table

Update(K, CT, ind, w; ST). Update is a protocol between the server and the client. Running this protocol, in the encryption way, a new file ind matching w is inserted into the inverted index with respect to keyword w, where ind denotes the file identifier with k bits length. Algorithm 2 provides a pseudo-code description of this protocol implementation.

Algorithm 2. Update(K, CT, ind, w; ST)

Output: system key master K, hash tables CT and ST, keyword w and file identifier ind
Output: updated hash tables CT and ST
Client: $w$
1: $K_w \leftarrow F(K, w[1])$, $K'_w \leftarrow F(K, w[2])$
2: (cnt, $I_1$) $\leftarrow$ CT[w].
3: if (cnt, $I_1$) $\leftarrow \bot$ then
4: $T_0 \leftarrow \{0, 1\}^{t_1}$, cnt $\leftarrow 0$
5: $(I_1, I_2, \{C_i, D_i\}_{1 \leq i \leq |S|}) \leftarrow \Gamma$.Enc
6: else
7: $R_{cnt} \leftarrow F(K_w, \cdot)$
8: $T_{cnt} \leftarrow H_3(k_w, R_{cnt})$
9: end if
10: $R_{cnt+1} \leftarrow F(K_w', \cdot)$
11: $T_{cnt+1} \leftarrow H_2(k_w, R_{cnt+1})$
12: $U_{cnt+1} \leftarrow T_{cnt} \oplus T_{cnt+1}$
13: $\text{ind} \leftarrow R_{cnt}[U_{cnt+1} || \text{ind}] \oplus H_4(K_w, R_{cnt+1})$
14: $\text{Send}(\text{ind}, T_{cnt}, T_{cnt+1}, \psi(I_1), T_1, \{C_i, D_i\}_{1 \leq i \leq |S|})$ to the server.
15: cnt $\leftarrow$ cnt + 1
16: $\text{CT}[w] \leftarrow (\text{cnt}, T_1)$
Server:
17: $(\mu, I_2, \{C_i, D_i\}_{1 \leq i \leq |S|}) \leftarrow \text{ST}[T_{cnt}]$
18: if $((\mu, I_2, \{C_i, D_i\}_{1 \leq i \leq |S|}) \neq \bot)$ then
19: $\text{ST}[T_{cnt}] \leftarrow \mu \oplus \psi(I_1)$
20: end if
21: $\mu \leftarrow \text{ind} \oplus \psi(I_1)$
22: $\text{ST}[T_{cnt+1}] \leftarrow (\mu, I_2, \{C_i, D_i\}_{1 \leq i \leq |S|})$

The client takes the master key K, the hash table CT, the keyword w, and the file identifier to be inserted ind containing w as input, the protocol generates two secret keys $K_w$ and $K'_w$ using the pseudo-random function F under the master key K, and proceeds as follows. The client retrieves CT[w] to take the number cnt of files currently containing w and w’s search permission component $I_1$. If keyword w appears for the first time, the client invokes $\Gamma$.Enc to encrypt w as ciphertext $T_w$(I_1, I_2, \{C_i, D_i\}_{1 \leq i \leq |S|}), sets a sentinel $T_0$ and initializes cnt to be 0 as well (lines 3-5). Recall that, in ABKS-NICE scheme, since the ciphertext $T_w$ contains the access policy determining who has permission to search w, here, we call $T_w$ the search permission of keyword w. Otherwise, it derives a pseudo-random value $R_{cnt}$ using F from $K'_w$ and cnt, and subsequently generates $T_{cnt}$ using $H_3$ from $K_w$ and $R_{cnt}$. The same operations are performed on cnt + 1 to generate $R_{cnt+1}$ and $T_{cnt+1}$. Here, the use of pseudo-random value $R$ (line 7 and line 10) is to guarantee forward privacy, and we will discuss this security issue in next section. Next, a new encrypted entity is formed ind containing information $R_{cnt}, T_{cnt} \oplus T_{cnt+1}$, and identifier ind (lines 12 and 13). Finally, cnt is incremented and (cnt, $I_1$) is stored in CT[w].

The server takes the hash table ST as input, it first tries to gain a value by retrieving ST[T_{cnt}]. If the value exists, this means ind is not the first file to be inserted containing w. The server doesn’t need to wipe the search permission component $I_w$ from current entity stored in ST[T_{cnt}] (line 19). Finally, the server generates a new entity u by associating $I_1$ with ind using a XOR operation (line 21), u along with the other two search permission components $I_2$ and $\{C_i, D_i\}$ is stored in ST at locations $T_{cnt+1}$ (line 22).

Algorithm 3. Search(K, CT, w; ST)

Input: system master key K, hash tables CT and ST, query keyword w
Output: a set rest of search results
Client: $w$
1: $K_w \leftarrow F(K, w[1])$, $K'_w \leftarrow F(K, w[2])$
2: (cnt, $I_1$) $\leftarrow$ CT[w].
3: if (cnt, $I_1$) $\leftarrow \bot$ then
4: return $\emptyset$
5: end if
6: $R_{cnt} \leftarrow F(K_w', \cdot)$
7: $T_{cnt} \leftarrow H_3(k_w, R_{cnt})$
8: $(I_1, I_2, \{T_u\}_{u \in S}) \leftarrow \Gamma$.TrapGen
9: $\text{Send}(K_w, R_{cnt}, T_{cnt}, I_1, T_2, \{T_u\}, \text{cnt})$ to the server.
Server:
10: rest $\leftarrow \emptyset$
11: $(\mu, I_2, \{C_i, D_i\}_{1 \leq i \leq |S|}) \leftarrow \text{ST}[T_{cnt}]$
12: if $(\exists \{\omega_i \in \mathbb{Z}_p^2 \mid i \in \{1, 2, \ldots, |S|\})$ then
13: $\chi \leftarrow e(I_2, I_1)/\prod_{i \in I_1} \left(e(C_iT_2T_eD_iT_{\rho(i)})\right)^{w_i}$
14: ind $\leftarrow \mu \oplus \psi(\chi)$
15: (ind, $U_{cnt}, R_{cnt-1}) \leftarrow \text{ind} \oplus H_4(K_w, R_{cnt})$
16: rest $\leftarrow \text{rest} \cup \{\text{ind}\}$
17: if cnt $\geq 2$ then
18: for c = cnt to 2 do
19: $T_{c-1} \leftarrow U_c \oplus T_c$
20: end if
21: $\text{ind} \leftarrow \text{ST}[T_{c-1}]$
22: rest $\leftarrow \text{rest} \cup \{\text{ind}\}$
23: end for
24: end if
25: end if
26: return rest

Search(K, CT, w; ST). Search is a protocol between the client and the server. Running this protocol, the server will return to the client a set of file identifiers matching w or an empty set. Algorithm 3 provides a pseudo-code description of this protocol implementation.
TABLE 2
Notations for Evaluation

<table>
<thead>
<tr>
<th>Notation</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \Delta )</td>
<td>keyword universe</td>
</tr>
<tr>
<td>( \Delta' )</td>
<td>authorized keyword set of a given search query, ( \Delta' \subseteq \Delta )</td>
</tr>
<tr>
<td>( P )</td>
<td>bilinear pairing operation</td>
</tr>
<tr>
<td>( F )</td>
<td>the set of data files</td>
</tr>
<tr>
<td>( E, E_T )</td>
<td>exponentiation operation in group ( G, G_T ), respectively</td>
</tr>
<tr>
<td>( H_i )</td>
<td>hashing a string to an element in ( G )</td>
</tr>
<tr>
<td>( S )</td>
<td>the set of attributes in an access policy</td>
</tr>
<tr>
<td>( U )</td>
<td>the data user’s attribute set</td>
</tr>
<tr>
<td>( \xi )</td>
<td>the least attribute set satisfying an access policy</td>
</tr>
</tbody>
</table>

The client takes the master key \( K \), the table \( CT \), and a query keyword \( w \) as input, two secret keys \( K_w \) and \( K'_w \) are derived from \( w \) and \( w' \), respectively. The protocol proceeds as follows. The client retrieves \( (\text{ent}, I_2) \) from \( CT \) \( |w| \) (If \( \text{ent} \) does not exist, the protocol will terminate in advance) and generates \( R_{\text{cont}} \) and \( T_{\text{cont}} \). Also, the client invokes algorithm \( \text{TrapGen} \) in ABKS-NICE to generate a search trapdoor \( T_w \) used to verify whether this search has permission to obtain the results containing \( w \).

The server takes the table \( ST \) as input and retrieves entity \( u \) matching \( w \) and \( u \)’s search permission components \( I_2 \) and \( \{C_1, D_1\} \). If the attribute set embedded in \( T_w \) satisfies the access policy associated with \( I_2 \) and \( \{C_1, D_1\} \), the server can obtain the \( \text{ent}^{th} \) file identifier \( \text{ind}_{\text{ent}} \), since (see \( \Gamma \). Match algorithm)

\[
e(I_2, T_1) = \prod_{i \in I} (e(C_i, T_2) e(D_i, T_{\rho(i)}))^{\alpha_i} = I_1 = \chi,
\]

\[
\mu \bigoplus \psi(\chi) = \text{ind} \bigoplus \psi(I_1) \bigoplus \psi(\chi) = \text{ind}.
\]

Decrypted \( \text{ind} \) to obtain \( (\text{ind}_{\text{ent}}, U_{\text{ent}}, R_{\text{cont}}{\text{-}1}) \) and add \( \text{ind}_{\text{ent}} \) into the result set \( \text{rest} \) (lines 15 and 16). Having \( U_{\text{ent}} = T_{\text{ent}} - 1 \oplus T_{\text{ent}} \), \( R_{\text{cont}} - 1 \), and \( T_{\text{cont}} \), by the XOR chain, the server iteratively obtains search results \( \text{ind}_{\text{ent}}{\text{-}1}, \text{ind}_{\text{ent}}{\text{-}2}, \ldots, \text{ind} \) (lines 18-22).

### 7.3 Performance

In order to highlight the practicality of ABKS schemes in the real scenario, we theoretically evaluate the computational performance trends of ABKS algorithms (especially the search efficiency) caused by the size of the index keyword universe. In the evaluation, for simplicity, we just consider heavy group operations in ABE environment (public-key setting), that is, the pairing operation, the exponentiation operation, and the hash operation \( H_1 \), while ignoring lightweight computations in symmetric cryptographic setting.

As a comparison, we evaluate the similar work proposed in [14], the only ABKS scheme so far that the authors use real-world data set to evaluate its search efficiency via a simple inverted index. Recall that ABKS-NICE is also an attribute-based keyword equality match scheme, and we generate a same index construction as scheme [14] in a real data set to evaluate its performance. Several notations are shown in Table 2. We describe the computational cost of each algorithm for different schemes in Table 3.

Table 3 demonstrates that ABKS-NICE, ABKS-NICEST, and scheme [14] have the asymptotically same computational complexity in terms of KeyGen and Enc algorithms, and the TrapGen algorithm in scheme [14] keeps the constant exponentiation operations and is relatively efficient compared with ABKS-NICE and ABKS-NICEST. Note that, in ABKS-NICEST, the algorithm KeyGen, Enc, TrapGen is invoked by Setup, Update, and Search, respectively. We can observe that the time-consuming exponentiation operation \( E \) and hash operation \( H_1 \) in Enc are linear with the size of the keyword universe (the asymptotic complexity is \( O(|\Delta|) \)), which will lead to a high computational overhead especially when the size of the keyword universe is large. However, to achieve retrieval on ciphertexts, the encrypted index construction may be a high price that any searchable encryption must pay for.

The search efficiency is of paramount importance in determining availability for a practical search system. Similar to scheme [14], given a search query, the expensive pairing and exponentiation operations in ABKS-NICE scale with the size of AKS of the search query. This is because those two schemes need to linearly scan the encrypted index keywords to obtain matched data files, which may lead to redundant search authorizations. As a result, the higher the search permission of a data user is, the higher the average search complexity is. An extreme case is that if a data user has the search permission of the whole index keyword universe, the average search complexity is \( O(|\Delta|) \). Note that ABKS-NICE has slightly better search efficient than scheme [14], as the pairing operations in ABKS-NICE are linear in \(|\xi|\), but \(|S| \) in Scheme [14], usually \(|S| > |\xi|\).

ABKS-NICEST has the optimal search efficient with complexity \( O(1) \) on both search query and search authorization, regardless of the size of the keyword universe.

### 7.4 Security

As an application case of structured encryption, ABKS-NICEST is a searchable encryption by structurally indexing encrypted data. Therefore, in the real-world service, ABKS-NICEST unavoidably leaks information to the cloud server (adversary) for pursuing a practical search efficiency. This

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<tbody>
<tr>
<td>KeyGen</td>
<td>((3 + |\xi</td>
<td>))E + |\xi</td>
<td>H_1)</td>
<td>((3 + |\xi</td>
</tr>
<tr>
<td>Enc</td>
<td>(</td>
<td>\Delta</td>
<td>(E_T +</td>
<td>S</td>
</tr>
<tr>
<td>TokenGen</td>
<td>((3 + |\xi</td>
<td>)E)</td>
<td>((3 + |\xi</td>
<td>)E)</td>
</tr>
<tr>
<td>Search</td>
<td>(1 + |\xi</td>
<td>((1 + 2|S|)E +</td>
<td>S</td>
<td>E_T))</td>
</tr>
</tbody>
</table>

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is also a generally existing tradeoff between security and efficiency for searchable encryption. Our goal is to minimize the leakages. Typically, this is captured via the standard security model of a real-world experiment $\text{RealExp}$ versus a ideal-world experiment $\text{IdeaExp}$. The security model is formalized by a group of leakage function $\mathcal{L} = (\mathcal{L}_{\text{Setup}}, \mathcal{L}_{\text{Update}}, \mathcal{L}_{\text{Search}})$, which specifies the upper limit of information that a dynamic searchable encryption scheme can reveal to adversary when running algorithm Setup and protocols Update and Search, correspondingly. We describe $\text{IdeaExp}$ and $\text{RealExp}$ experiments as follows.

- $\text{RealExp}_A(k)$: A PPT adversary $A$ chooses a set of data files $DB$, the experiments first runs algorithm $\text{Setup}(k; L)$ and returns $ST$ to $A$. Then, $A$ performs search and update queries for polynomially-bounded times and receives a series of transcripts generated from Search and Update protocols. $A$ observes these results and outputs a bit $b \in \{0, 1\}$.

- $\text{IdeaExp}_A,k(\mathcal{L})(k)$: A PPT adversary $A$ chooses a set of data files $DB$, there exists a simulator $S$ that runs the leakage function $\mathcal{L}_{\text{Setup}}$ and returns $S(\mathcal{L}_{\text{Setup}}(k; L))$ to $A$. Then, $A$ performs search and update queries for polynomially-bounded times and receives a series of transcripts generated from the simulator $S(\mathcal{L}_{\text{Search}}(w))$ and $S(\mathcal{L}_{\text{Update}}(\text{ind}, w))$. $A$ observes these results and outputs a bit $b \in \{0, 1\}$.

We say a searchable encryption is $\mathcal{L}$-adaptively-secure searchable encryption if for any PPT adversary $A$, there exists a PPT simulator $S$ such that:

\[
\text{Pr}\left(\text{RealExp}_A(k) = 1\right) - \text{Pr}\left(\text{IdeaExp}_A,k(\mathcal{L})(k) = 1\right) \leq \text{negl}(k),
\]

where $k$ is a security parameter and $\text{negl}(k)$ is a negligible function in $k$.

**Theorem 3.** Given the pseudo-random function $F$, when modeling $H_3$ and $H_4$ as a random oracles, if $q$-parallel BDHE assumption holds, our proposed ABKS-NICEST is a dynamic $\mathcal{L}$-adaptively-secure searchable encryption scheme.

Refer to Appendix C to find the complete proof.

**Forward Privacy:** Forward privacy claims that all search queries that have been issued before cannot be used to gain the newly added data files that are being updated. This property guarantees a update query cannot leak any keyword information in the newly added data, radically resists the file injection attack. Our proposed ABKS-NICEST achieves forward security since in Update protocol (Algorithm 2) we designedly introduce the pseudo-random value $R$ with secret key $K'$. Without $K'$, the server cannot generate up-to-date $R_{\text{cnt}+1}$ and $T_{\text{cnt}+1}$ from pervious counters $1, \ldots, \text{cnt}$ ($K'$ has been never given to the server). As a result, the newly updated data files cannot be searched using pervious search queries.

## 8 Experimental Evaluation

We experimentally evaluate ABKS-NICE and ABKS-NICEST in a real data set Enron Email Dataset.\(^1\) As a comparison, we also implement the similar work ABKS-HD\(^{[13]}\) and scheme\(^{[14]}\) that the authors use inverted index construction to evaluate performance on real data set. All programmes are run at Java platform with JPBC\(^2\) library and a Windows 7 with 3.30 GHZ Inter Core i7-11370H CPU, 16 GB memory. Our implementation uses the symmetric bilinear map Type A over a 160-bit elliptic curve group.

### 8.1 Efficiency for Key and Token Generation

In this section, we evaluate the efficiencies of algorithms $\text{KeyGen}$ and $\text{TokenGen}$ with varying number of data user’s attributes. Fig. 8 shows a performance comparison among ABKS-NICE, ABKS-NICEST, ABKS-HD and Scheme \(^{[14]}\). We can observe that the time cost of all of the four schemes increases with the increasing number of attributes. ABKS-NICE and ABKS-NICEST have approximate computational cost to generate a private key, while ABKS-HD and Scheme \(^{[14]}\) need slightly more time. For example, when setting $|U| = 20$, ABKS-NICE, ABKS-NICEST, ABKS-HD, and Scheme \(^{[14]}\) spend about 0.6 s, 0.601 s, 0.7 s, and 0.768 s on the private key generation, respectively. These results

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are also in accordance with the theoretical evaluation in Table 3.

Fig. 9 shows the time cost of encrypting a search keyword when varying the number of data user's attributes. The experimental results show that Scheme [14] requires expending least cost to generate search trapdoor, and is moreover not affected by the number of attributes, while ABKS-NICE, ABKS-NICEST, and ABKS-HD grow linearly. These experimental results conform with the theoretical analysis for the TokenGen algorithm in Table 3. For example, \( |U| = 20 \), ABKS-NICE, ABKS-NICEST, ABKS-HD, and Scheme [14] consume about 0.193 s, 0.189 s, 0.451 s, and 0.018 s, respectively.

### 8.2 Evaluation for Secure Index Construction

We extract 600 index keywords from 4000 data files in Enron Email Dataset. In practice, different index keywords should be specified personalized access policies to indicate their search permissions. However, a variety of structures of access policy raise the difficulty for our evaluations, especially for the search performance evaluations. Therefore, in our experiments, we use for all keywords unified access policy structure as “a1 AND a2 AND... a_l,” where \( a \) denotes an attribute and \( l = 20 \). Its corresponding access tree (used in ABKS-HD and Scheme [14]) and LSSS matrix (used in ABKS-NICE and ABKS-NICEST) are shown in Fig. 10.

Fig. 11a shows the time cost of encrypting index keywords when varying the size of index keywords with fixed number of data files (\( |F| = 4000 \)). Our experimental results show that the cost of constructing secure index of all of the four schemes linearly increases with the number of index keywords. ABKS-HD needs much more time over-head than other three schemes, and ABKS-NICE and ABKS-NICEST have approximate computational overhead and are more than that of Scheme [14]. This is because ABKS-HD includes \( 2|\Delta||S| + 2|F||S| \) exponentiations, and ABKS-NICE and ABKS-NICEST include \( 3|\Delta||S| \), but \( 2|\Delta||S| \) in Scheme [14]. Compared to ABKS-NICE, ABKS-NICEST needs a little more time due to a number of light-weight computations such as XOR and hash operations. The second group experiment is to vary the number of data files and fix the size of index keywords (\( |\Delta| = 500 \)). Fig. 11b demonstrates that ABKS-NICE, ABKS-NICEST, and Scheme [14] are not affected by the size of data files, but the time cost in ABKS-HD linearly grows. The results show that secure index construction is an extremely expensive process.

Figs. 11a and 11b demonstrate the one-time cost on index construction over a static data set. However, in the real-world application, for ABKS-NICEST scheme, the every-time cost required to expend on index keyword encryption will far less the above experimental results, as ABKS-NICEST is dynamic. Practically, the index keywords are encrypted in batches in the different update time point (File Update Window, FUW). Fig. 11c shows a group of experimental results for the different file update windows. In the current FUW, only these index keywords that have not appeared in the previous FUW need to be encrypted (See Algorithm 2, lines 2-5). Generally speaking, in the first update (FUW-1), the time cost of index construction achieves maximum, as all keywords appear for the first time. In the subsequent FUW, many keywords have been encrypted in the previous FUW, the time cost is drastically reduced.

### 8.3 Evaluation for Data Search

For ease of evaluation and comparison, we set \( |\xi| \) to be identical to \( |S| \) and let any search query have the search permissions of all index keywords, i.e., set \( |\xi| = |S| = |U| = 20 \). This is equivalent to a simulation that a super data user conducts data searching.

Fig. 12a demonstrates when varying the size of index keywords and fixing the number of data files, the time cost distributions of the search algorithms in ABKS-NICE, ABKS-NICEST, ABKS-HD, and Scheme [14]. In this evaluation, we perform 6 groups experiments with an incremental size of index keyword set. We repeat to perform 30 times search in each experiment, and choose query keywords from the currently incremental index keywords. For example, in the first group, the 30 query keywords are randomly chosen from range \( [0,100] \) (i.e., set \( \{w_1, \ldots, w_{100}\} \)), and second group is \( [101,200] \), and so on. The intention of choosing query keywords in this way is to observe the impact of the size of index keywords set on search efficiency. We can see that the time cost of ABKS-NICE, ABKS-HD, and Scheme [14] emerge an explicitly linear increase with the size of the index keyword set, while ABKS-NICEST is not affected by the number of index keywords. Fig. 12b shows that, when varying the size of Oct 16, 2023 at 15:54:27 UTC from IEEE Xplore.
data files and fixing the number of keywords, the time cost distributions of the search algorithms in ABKS-NICE, ABKS-NICEST, ABKS-HD, and Scheme [14]. In order to focus on the impact the size of data file set on search efficiency, we select query keywords from range [200,400]. This can effectively circumvent possible linear distribution of experimental results due to linearly choosing query keywords, which has been evaluated in Fig. 12a.

The remarkable conclusion is that, for ABKS-NICEST, the sizes of both data file set and index keyword set have very little influence on the search overhead; more importantly, the search time near to 0.06 s is extremely efficient, while in ABKS-NICE, ABKS-HD, and Scheme [14] the search complexities are too high to be accepted in practice. For example, in the worst-case, running a search needs to spend about 160 s in ABKS-NICE, ABKS-HD, and Scheme [14]. Practical search efficiency is crucial for the availability of a real-world search system.

9 Conclusion
In this paper, we investigate the attribute-based keyword search over encrypted cloud data. First, we construct an ABKS scheme supporting numeric attribute comparison policy, namely ABKS-NICE. Similar to the existing schemes, ABKS-NICE is static and with an impractical search complexity. Based on ABKS-NICE and our proposed encrypted XOR chain, we design the first truly practical and dynamic ABKS scheme, ABKS-NICEST. By the theoretical and experimental performance evaluations, ABKS-NICEST is most efficient ABKS scheme with dynamic data update ability as far as we know. Also, we provide formal security proofs for ABKS-NICE and ABKS-NICEST. As our future work, we will research practical and dynamic multi-keyword ABKS scheme, ABMKS-NICEST.

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References

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